ADDENDUM

for *Topics in Spectral Geometry*, preliminary online version dated May 29, 2023

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deletions are shown in red, and additions/replacements in green

- ☞ **p. 28, two lines above Remark 1.2.14:** since an issue with the preprint [BouWat17] became known in July 2023, the best existing upper bound for $R(\lambda)$ has exponent $\frac{131}{416}+\varepsilon<0.315$ [M. N. Huxley, *Exponential sums and lattice points III*, Proc. London Math. Soc. (3) **87** (2003), 591–609. doi: 10.1112/S0024611503014485]

- ☞ **p. 68, above Exercise 3.1.6:** on reflection, the phrase "Proposition 3.1.3 follows immediately" is somewhat misleading. Therefore, for methodological purposes, we extend the argument outlining the proof of Proposition 3.1.3. Let $\mathscr{E}_k := \operatorname{Span}\{u_k, u_{k+1}, \dots\}$. Then $R[u] \ge \lambda_k$ for any $u \in \mathscr{E}_k \setminus \{0\}$. If we now consider an arbitrary $\mathscr{L} \subset \operatorname{Dom}(\mathscr{Q})$ with $\dim \mathscr{L} = k$, then there exists $u \in \mathscr{E}_k \cap \mathscr{L} \setminus \{0\}$ (since the codimension of $\mathscr{E}_k$ is $k-1$), and therefore

$$\max_{u\in\mathscr{L}\setminus\{0\}} R[u] \ge \lambda_k.$$

  On the other hand, the equality is attained if we take $\mathscr{L} = \operatorname{Span}\{u_1, \dots, u_k\}$.

- ☞ **p. 314, reference [BerGMR21]:** add full bibliographical data, J. Math. Anal. Appl. **538**:2 (2024), 128460. doi: 10.1016/j.jmaa.2024.128460

- ☞ **p. 317, reference [ColGGS22]:** add full bibliographical data, Rev. Mat. Complut. **37** (2023), 1–161. doi: 10.1007/s13163-023-00480-3

- ☞ **p. 319, reference [FilLPS23]:** add full bibliographical data, Invent. Math. **234** (2023), 129–169. doi: 10.1007/s00222-023-01198-1

- ☞ **p. 324, reference [KarLagPol22]:** add full bibliographical data, Arch. Rational Mech. Anal. **47** (2023), article no. 77. doi: 10.1007/s00205-023-01912-6

- ☞ **p. 324, reference [KarSte20]:** add bibliographical data, J. Eur. Math. Soc. (2023). doi: 10.4171/JEMS/1401

- ☞ **p. 324, reference [KarSte22]:** add full bibliographical data, Invent. Math. **236** (2024), 713–778. doi: 10.1007/s00222-024-01247-3
- ☞ **p. 330, reference [NurRowShe19]:** add bibliographical data, Ann. Math. Québec (2024). doi: 10.1007/s40316-024-00237-4
- ☞ **p. 331, reference [Ros22b]:** add full bibliographical data, Math. Z. **305** (2023), article 62. doi: 10.1007/s00209-023-03382-8
- ☞ **p. 332, reference [Roz23]:** add full bibliographical data, J. Spectr. Theory **13**:3 (2023), 755–803. doi: 10.4171/JST/477